

- 1 9:49 Bill: Okay, let me get some scratch paper there. Can we use that for scratch?
- 2 Ann: Yeah. Probably.
- 3 Bill: Let me see what it is. Looks to me like that's scratch paper. Okay, Let me get my
4 stuff together here while that's coming up. Okay this is kind of like a...simulated
5 race, in this over and back. It's a race between a turtle and a rabbit [*points to them on*
6 *the computer screen*]. And to be able to make these things operate all we need to do is
7 to come over here and press run turtle or run rabbit or run both [*points to the on-*
8 *screen Buttons*]. We can do them individually like you see or we can run them both at
9 the same time. The other things that are on the screen here, you see here's the turtle,
10 an arrow going to the right, and a turtle with an arrow going to the left, and then the
11 just plain rabbit, and then time [*points to these words in turn on the computer screen*].
12 What this means [*points to the Turtle-Over Box*] is that we can set the speed that the
13 turtle is going to run in that direction only [*moves hand quickly over distance line*].
14 And we can set the speed [*points to the Turtle-Back Box*] for it to come back [*moves*
15 *hand back along the distance line*], but for the turtle we have to set both speeds. For
16 the rabbit we just have one. Whatever we're setting for he goes over and back at the
17 same speed [*moves hand over and back*]. Okay? That's really all it is [*gestures to the*
18 *computer*]. Pretty simple, huh [*Ann nods*]? So before we get on to that, I want to ask
19 you though, we're going to be talking about speeds [*points to the Turtle Boxes*] here
20 in feet per second, but...can you tell me what it means to you if you're riding in the
21 car with your folks and they're driving at forty-five mph? What does that mean to
22 you?
- 23 9:51 Ann: It means, like...it means, like, if you're going forty-five miles per hour that means
24 that if you time yourself at an hour you would have gone forty-five miles from where
25 you started.
- 26 Bill: Good. That's true. How about if you only went a half hour? Instead of driving for an
27 hour you drove for thirty minutes.
- 28 Ann: For a half hour?
- 29 Bill: Yeah.
- 30 Ann: You would only go half of forty-five.
- 31 Bill: Very good. Umm...well, that's in effect what we're doing here [*points to the*
32 *computer*] except the distances we have here are in feet [*points to 100 ft at the end of*
33 *the distance line*] and instead of miles per hour here we're going to have feet [*points*
34 *back to 100 ft and then quickly to the Time Counter*] per second. Okay?
- 35 Ann: Okay.
- 36 Bill: So, as an example, if we take the turtle here [*points to the Turtle-Over Box*], which it
37 currently shows that he's set for thirty, what does that mean?
- 38 Ann: [*Short pause*] Thirty feet per second?
- 39 9:52 Bill: [*Nods*] Uh huh.
- 40 Ann: [*Pause*] So, he wouldn't go that far...right?

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- 41 Bill: Yeah, but...and we were talking about miles per hour before, here we have thirty feet
42 per second for the turtle [*again pointing to the Turtle-Over Box*]. What does that
43 mean to you in terms of his speed?
- 44 Ann: He'll go thirty feet in one second.
- 45 Bill: Good. How far will he go in two seconds?
- 46 Ann: Sixty feet.
- 47 Bill: Very good. Pretty simple isn't it? [*Ann nods*] Okay. Well, let's start off, I can show
48 you how to do these things [*reaches over and grasps the mouse*], but you see this
49 arrow, I can comment that you've been using this before, I can either use the mouse
50 to set those or I can use the tab keys. [*Taps the tab key three times*] You see I can
51 move the tab key and it moves it to the different areas? And all I have to do is go up
52 and put in the number [*types "20" into the Turtle-Over Box*] and I don't even have to
53 hit enter, okay. So then I'm going to set the turtle for twenty going that way, and
54 twenty...coming back [*types "20" into the Turtle-Back Box*]. Do you understand
55 what I've done now, in effect?
- 56 Ann: [*Nods*] Yeah.
- 57 Bill: He's going to go this way at twenty feet per second, and when he hits the end he's
58 going to turn around and come back [*moves finger over distance line, then back*].
59 Okay? [*Ann nods slightly*] If I've set him for that [*waves hand towards the computer*],
60 can you tell me about how long it's going to take him to go over and back [*gestures*
61 *over and back along the distance line*]?
- 62 9:53 Ann: At twenty feet per second?
- 63 Bill: Uh huh.
- 64 Ann: These are in tens aren't they [*points to random tick marks*]?
- 65 Bill: Well, let's see. If this in a hundred out there [*points to 100 ft on the distance line*],
66 how do you think that [*moves hand back along distance line*] might be divided up?
- 67 Ann: Into tens.
- 68 Bill: Pretty good to me.
- 69 Ann: [*Pauses, staring at the computer screen*] Okay, so h-how long would it take him?
- 70 Bill: You can use paper by the way, too and the calculator [*picks up and puts back the*
71 *calculator*]. Don't hesitate to use either one.
- 72 Ann: [*While Bill was saying the last two sentences, Ann was gesturing over and back on*
73 *the table and asking:*] Go back ----? Go back and forth?
- 74 Bill: Yeah, how long will it take him to go over and back?
- 75 Ann: [*Stares at the computer. Then writes 100÷20 in long division form on her scratch*
76 *paper. Then she writes "5" as her answer*] Five seconds.
- 77 Bill: To go both directions, or just one way?
- 78 Ann: Just one way.

- 79 Bill: Very good, how did you get that?
- 80 Ann: I divided twenty into a hundred.
- 81 9:54 Bill: [*Nods*] Super. Can you tell me then how long it would...see he goes...[*gestures with hand over and back*] the race is like a relay race except each person runs by themselves.
- 82 He runs all the way over, and he turns around and runs right back, too [*moves finger over and back*].
- 83
- 84
- 85 Ann: So, it would be ten seconds if he went...[*waves hand over and back*].
- 86 Bill: 10 seconds. And you got that by dividing twenty into...
- 87 Ann: A hundred.
- 88 Bill: In this case you got that [*glances down at Ann's paper*] by dividing twenty into one
- 89 hundred, right? Very good. Should we try it and see?
- 90 Ann: Okay.
- 91 Bill: Let's run the turtle and see what happens. [*Ann activates the turtle*] There he goes.
- 92 You see that little counter down here [*pointing to Time Counter*] is keeping track of
- 93 our time. Bingo. Right on the money. Good job. Let me ask you this, if we set the
- 94 rabbit for twenty-five meters per second [*types in "25" into the Rabbit-speed Box*],
- 95 how long will it take him to go over and back?
- 96 Ann: [*Writes $100 \div 25$ on scratch paper*] Hmm... [*grabs calculator and types $25 \div 100$*]
- 97 Twenty-five hundredths of a second [*looking to Bill*]?
- 98 9:55 Bill: I don't think you divided right.
- 99 Ann: I didn't think so.
- 100 Bill: What you have on paper is probably correct. Twenty-five into one hundred. So here
- 101 you'd put in one hundred divided by...[*Ann tries but fails to use the calculator for*
- 102 $100 \div 25$] there you go... you hit the wrong button.
- 103 Ann: One hundred divided by...[*successfully uses the calculator for $100 \div 25$*] equals four?
- 104 [*Looks quizzically at Bill, then at computer, then writes "4" above the long division*].
- 105 Bill: [*Pause*] So what does that tell you there? Twenty-five into one hundred is four.
- 106 Ann: That it would be four seconds...for...one way across
- 107 9:56 Bill: Okay. [*draws a distance line below her long division work*]. That seems to
- 108 puzzle you. Why is that?
- 109 Ann: I don't know. [*Pause*].
- 110 Bill: Okay.
- 111 Ann: [*Counts the tick intervals by tapping pencil first three, then four times*] Yeah [*nods*].
- 112 Bill: Wha-what seems strange to you?
- 113 Ann: [*Shrugs shoulders*] I don't know. I just didn't understand.
- 114 Bill: You mean the twenty-five didn't sound right or what?
- 115 Ann: The four seconds.

- 116 Bill: Oh, four seconds.
- 117 Ann: Yeah.
- 118 Bill: Is it too long or too short, do you think?
- 119 Ann: [*Shrugs slightly, then lowers gaze*] I thought it was too short. Sounds too short.
- 120 Bill: Well, we are looking [*Ann says something unintelligible*] for the time it takes him to
121 go both over and back, so how long is that going to take him?
- 122 Ann: That would take him eight seconds.
- 123 Bill: Eight seconds, do you want to give him a try? [*Ann activates rabbit, who finishes in*
124 *eight seconds*]. You're right on the money. Very good. You had a frown on your face,
125 what were you puzzled about there?
- 126 9:57 Ann: [*Shrugs, then pauses*] Just wondering [*moves the mouse back and forth while*
127 *watching the computer screen*] how they can make him move back and forth so
128 quickly.
- 129 Bill: Oh, how does the program do it?
- 130 Ann: Yeah [*laughing*].
- 131 Bill: You'll have to ask Dr. Thompson about that. I don't know. I didn't write the program.
132 Let's take another step now. Hey, we're buzzing right along here. Let's say we leave
133 the turtle going over at twenty meters per second, err, I'm sorry feet per second and
134 you want to change that one [*note: Turtle-Back Box*] to fifty. Plug in fifty there [*Ann*
135 *types "50" into the Turtle-Back Box*]. And then you know what I'm going to ask you.
136 How long is it going to take the turtle to go over and back [*waves finger over and*
137 *back*]?
- 138 Ann: Four seconds.
- 139 Bill: [*Looks to the computer screen, then to Ann*] Okay. How did you come up with that?
- 140 Ann: Because half of a hundred is fifty, so it would be two fifties to equal one hundred.
- 141 Bill: Okay.
- 142 Ann: And then two plus two is four.
- 143 Bill: Okay, but remember he's going over [*points to the Turtle-Over Box*] at twenty feet
144 per seconds.
- 145 9:58 Ann: Yeah [*laughs*]. Okay, so it'll take him twenty to get back...or fifty. [*Writes "2 sec.*
146 *get back" then looks at the computer screen. She then writes "+5" under the 2.*]
147 Eight [*writes "8" under the addition column*]. It would take him eight seconds
148 because it would take him five seconds to take him across [*moves pencil over in the*
149 *air*] through twenty.
- 150 Bill: Okay [*nods*]. And how did you get the five...the five seconds?
- 151 Ann: Because I already did it up here [*circles the $100 \div 20 = 5$ long division problem on the*
152 *scratch paper*].
- 153 Bill: Ah, from earlier work. Okay, so our total time was going to be what?

- 154 Ann: Eight seconds.
- 155 Bill: And that's these two added together [*reaches over and points to 2+5*]?
- 156 Ann: Yeah. [*Note: The 2 could possibly be misinterpreted as a 3 due to the way Ann wrote*
157 *the number.*]
- 158 Bill: Five plus two?
- 159 Ann: Seven [*Bill winks*]...eight same thing.
- 160 9:59 Bill: [*Looks surprised*] Oh, okay, the same thing.
- 161 Ann: Close [*scribbles a "7" over the 8*].
- 162 Bill: [*Chuckles*] All righty. Do you want to try it? Let's see [*Ann activates turtle*]. You said
163 five seconds to get there right? Bingo, Looks like you're right on. Look at him go
164 right back. Wee! How about that [*Ann nods slightly*]? Good, let's do this now. Let's
165 skip one down and set the...turtle [*types "30" for the Turtle-Back Box*] for
166 thirty...and have you do the same thing.
- 167 Ann: How long would it take him to get back?
- 168 Bill: Over and back.
- 169 Ann: Over and back. We already know it will take him five seconds with the twenty.
- 170 Bill: Okay.
- 171 Ann: So thirty into a hundred instead. [*Writes 100÷30 in long division form. Then uses the*
172 *calculator. Looks at the calculator display, then to Bill*] I don't think I did that right
173 [*giggles*].
- 174 Bill: Why? What did you come up with? What did you do and then what did you come up
175 with?
- 176 10:00 Ann: [*Reading off of the calculator display*] 333333333.
- 177 Bill: [*Reaches over and looks at the calculator display*] Is there a decimal in there
178 somewhere?
- 179 Ann: Yeah.
- 180 Bill: Yeah. So what...isn't this...what is this, seconds we're dealing with?
- 181 Ann: Yeah.
- 182 Bill: So how long would that be?
- 183 Ann: That would be...three seconds [*looks at the calculator display, counting the threes*
184 *after the decimal point*] and ten million. Three thousand and ten millionth.
- 185 Bill: Oh, I see. No. Let's forget about all those other threes back there [*points to the*
186 *calculator display*].
- 187 Ann: Three seconds.
- 188 Bill: Why don't we just say it's going to be...because here [*points to the Time Counter*]
189 we're only measuring to the first decimal place.
- 190 Ann: Yeah.

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- 191 Bill: The tenths place. So why don't we look only at the tenths place here [*again pointing*
192 *to the calculator display*]. We'll round to that and call it 3.3.
- 193 Ann: 3.3 [*writes "3.3" over long division $100 \div 30$*].
- 194 Bill: Okay. And then your total time over and back?
- 195 Ann: [*Writes $5 + 3.3$ in column form. Rewrites the 5 so that the decimal points align. Then*
196 *adds them and writes "8.3"*] 8.3 seconds.
- 197 10:01 Bill: Let's see [*Ann activates turtle*]. And again you got that by dividing thirty into the
198 hundred, right?
- 199 Ann: Yeah.
- 200 Bill: Very good. [*Race ends*] Looks to me like you're pretty accurate. See what it says here
201 [*pointing to the Time Counter*]? Let me show you also what we can do up here in the
202 options menu, just to...make it a little bit interesting [*uses the mouse to add digits*
203 *onto the Time Counter*]. See there's the additional 333333s. If I had more places I
204 would continue to get them all the way across. Okay. So you're right on the money.
205 That's very good Ann. Let's go back to that position [*uses the mouse to have the Time*
206 *Counter display only to the tenths place*]. I want to set them now for the...turtle to go
207 forty [*types "40" in the Turtle-Over Box*]. And that's forty over and he's going to go
208 twenty back [*Bill types "20" in the Turtle-Back Box. Ann writes $100 \div 40$ in long*
209 *division form*]. And the rabbit now is going to race him, and we're going to set the
210 rabbit for twenty-five...feet per second [*rabbit stays at 25*].
- 211 Ann: So how long would it take each of them to go over and back?
- 212 10:02 Bill: Who's going to win the race? [*Pause*] Why don't you go ahead [*points to extra*
213 *scratch paper which Ann ignores*] and use a separate sheet if you want so we can kind
214 of keep this stuff organized if you want.
- 215 Ann: [*Ann draws a box around the $100 \div 40$. Then she uses the calculator for $100 \div 40$.*]
216 Aaagh [*makes a mistake and recalculates. She then writes "1st .025" and below that*
217 *"2st 2.5"*]
- 218 Bill: Make sure your decimal points...you're reading them correctly off of the
219 uh...calculator.
- 220 10:03 Ann: [*Moves the decimal to .25 on "1st." The she uses the calculator for $2.5 + 5.0$ and*
221 *writes, in an addition column labeled "T", $2.5 + 5.0 = 7.5$ in column form. Then she*
222 *writes "R" and under that "25" which she circles and boxes. Next to that, Ann writes*
223 *$4 + 4 = 8$ in column form, circles the problem, and draws an arrow to the 25.] The*
224 turtle will win.
- 225 Bill: He'll win, by how much?
- 226 Ann: By...five tenths of a second [*she says it half answer, half question*].
- 227 Bill: Okay. Do you want to run them [*gestures to the mouse*]? Let's see [*Ann activates*
228 *race*]. While they're running can you explain to me how you got your answer? How
229 did you come about deciding that they would win by that much?

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- 230 10:04 Ann: Okay...*[looking down at her work]* I tried to do a hundred into forty *[points with*
231 *pencil to her $100\div 40$ in long division form]* for...for the first time for the travel...that
232 the turtle *[gestures to the computer screen]* would travel.
- 233 Bill: Uh huh *[nods]*.
- 234 Ann: And then, when I got...it took me two tries, but when I got 2.5 *[points to the column*
235 *labeled T]*, I added that plus the five that I knew I would already have, the same thing
236 going back up *[draws a squiggly line from the T column to the first problem she*
237 *worked on, $100\div 20=5$ in long division form]* to here again.
- 238 Bill: Yeah, okay.
- 239 Ann: And then for twenty-five...
- 240 Bill: So, you figured out the turtle's total time was seven and a half seconds?
- 241 Ann: Yeah.
- 242 Bill: I see that *[glancing over at Ann's paper]*. Yeah, okay.
- 243 Ann: And then I took the twenty-five *[draws a line from the 25 under the R to the second*
244 *problem, $100\div 25=4$, and circles it]* and I went back to what...to the information I got
245 up here.
- 246 Bill: Ah, good for you.
- 247 Ann: *[mumbles something]*.
- 248 Bill: So it would take the rabbit eight. Unfortunately, I started you explaining that when
249 they were running the race, but uh...looks like something came up to eight seconds
250 *[gestures to the Time Counter]*, but I'm not sure which one it was. Should we run
251 them again just to see?
- 252 Ann: Okay.
- 253 Bill: I think it continues to run even after the turtle wins or the rabbit wins, but let's see
254 *[Ann activates race again and they watch. The turtle wins by half a second]*. Yep,
255 looks like you were right.
- 256 Ann: Yeah, ---- turtle.
- 257 10:05 Bill: Good for you. Okay, do you want to try one more of those?
- 258 Ann: Okay.
- 259 Bill: Let's try one with thirty for the turtle's speed going over and forty coming back. And
260 this time we're gonna set... oops, I don't want thirty...forty, forty coming back and
261 the rabbit we're going to set at thirty-five *[sets the Turtle-Over Box to 30, the Turtle-*
262 *Back Box to 40, and the Rabbit-speed Box to 35. Ann writes, in the upper right*
263 *portion of the scratch paper, $100\div 30=3.4$ and $100\div 40=2.5$ in long division form, and*
264 *then writes $3.4+2.5=5.9$ in column form. Her $100\div 30=3.4$ is only two inches from a*
265 *previous problem, $100\div 30=3.3$].*
- 266 Ann: Forty, thirty-five?
- 267 Bill: Yeah, he's going to come over and back at thirty-five. *[Note: referring to the rabbit.]*

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268 Ann: [*Writes $100 \div 35$ in long division form. She then uses the calculator and writes "2.8"*
269 *over the new division problem.*] This time the rabbit would win.

270 10:06 Bill: And his time is going to be?

271 Ann: His time would be 2.8.

272 Bill: Hmm. Okay.... You want to run them and see? [*Ann activates race*] You were right,
273 the rabbit won....But his time was a little bit different. How was that?

274 Ann: I just took the first two here [*points to the calculator display*].

275 Bill: [*A pause, then looks over to the display*] The other ones were just decimal places,
276 right?

277 Ann: Yeah, they were just...

278 Bill: Yeah, so we just round those off, but how far did he run in [*points toward Ann's*
279 *paper*] 2.8 seconds?

280 10:07 Ann: He...got all the way across [*moves finger over the distance line*] and he was coming
281 back. He was about there...[*points to middle of the distance line*] when he stopped.

282 Bill: Ah.

283 Ann: When he got to 2.8.

284 Bill: [*Slowly*] Okay. [*Pause*] Why don't you run the rabbit just by himself, so that way we
285 can kind of test, right? And see what goes on [*Ann activates rabbit*]. What did that tell
286 you?

287 Ann: Oh, I get it. I didn't add it up.

288 Bill: Yeah.

289 Ann: I should have [*scratches out the $100 \div 35$ long division*].

290 Bill: Why would that be?

291 Ann: Huh?

292 Bill: What was wrong with your calculations?

293 Ann: I needed to double it.

294 Bill: Why?

295 Ann: To get over and back.

296 Bill: Ah, you just calculated it over.

297 Ann: I went one way.

298 Bill: Okay, good. I'll tell you what, it looks like you've got this thing wired, so I want you
299 to see if you can work these out [*hands Ann a problem set*] and you're welcome to
300 write on this paper or on your own scratch paper if you want. Now what here I would
301 like you to do is let's just start off at the top, you can probably already figure out
302 some of these anyway. What's the rabbit's speed have to be to give me these times
303 [*points to left and right columns on problem set with pencil*]? Over and back, now

- 304 remember. And we can test him on there [*gestures toward computer*], or you can test
305 it on there if you like.
- 306 10:08 Ann: [*Pause*] Okay. [*Pauses. Writes what looks like $100 \div 5 = 2.8$ in long division form*
307 [*Note: perhaps in confusion over $100 \div 35$?*]. *Draws a line over and back above a*
308 *half-distance line she used previously, circles $100 \div 5$, then scratches it all out. Writes*
309 *$100 \div 5$ in long division form again. Types on calculator $100 \div$, stops and looks to the*
310 *paper, then back to the calculator.] Ohhh. [*Scratches out the long division. Writes*
311 *"100" and below that "5". Runs out of room on the scratch paper, so turns it over.]**
- 312 10:09 Bill: Here [*points to pile of scratch paper*], just grab another piece. There you go.
- 313 10:10 Ann: [*Spends much of her time staring at paper or tapping the desk with her pencil. Then*
314 *she draws a number line, dividing it up into three tick intervals*]
- 315 Bill: Gotta give you some more room there, you're almost off the table [*moves the*
316 *calculator, mouse and keyboard so that there is more desk space. Ann draws a new*
317 *number line under the first, this time eleven tick intervals long] You want to change
318 one?*
- 319 Ann: Yeah.
- 320 Bill: The rabbit? [*Ann nods*] Okay. All you've got to do is put in your number.
- 321 Ann: I'm almost sure I'm wrong, though.
- 322 Bill: What's an easy way to find out?
- 323 Ann: [*Chuckling*] I don't know [*Note: about the answer, not the "easy way to find out"*].
- 324 Bill: What speed do you think he should go at?
- 325 Ann: Fifty...probably [*types in 50 for the Rabbit-speed Box*].
- 326 Bill: Okay, and before you push the go line, why fifty? I mean, how did you come up with
327 fifty?
- 328 Ann: It seemed logical? I don't know [*shrugs shoulders*]...It's a guess.
- 329 Bill: Did that [*note: the 50*] have something to do with your drawings [*points to Ann's*
330 *scratch paper*] there?
- 331 10:11 Ann: No. I messed them up, I did it wrong.
- 332 Bill: Okay. Well, let's take a run at it. Let's see what it is. He really zips doesn't he?
- 333 Ann: Forty.
- 334 Bill: Why forty?
- 335 Ann: Because if it took four seconds at fifty, then if you subtract ten, it might take him a
336 whole second longer to get back.
- 337 10:12 Bill: Okay, he hung up, we'll see if he goes, there he you go.
- 338 Ann: Smiley face, I do it a lot.
- 339 Bill: You got it, right?
- 340 Ann: Yeah.

- 341 Bill: Okay, we'll write that in here and go on to the next one.
- 342 Ann: [*Reading off of problem set, whispering:*] 10 seconds.
- 343 Bill: The next one is ten seconds, right?
- 344 Ann: Oh, um,...I know how you get the answer, but [*chuckling*] I don't know how fast
- 345 [*presses "clear" on calculator repeatedly*].
- 346 Bill: How would you get it?
- 347 Ann: You would, umm...see if these [*points to the tick marks*] were split up in ten sections
- 348 it would take a second to get over each [*moves hand over and back*].
- 349 Bill: Okay, remember now we're talking over and back [*moves hand over and back*].
- 350 10:13 Ann: So, it would take five seconds. So, it's [*writes 5+5 in column form. Draws a number*
- 351 [*line with five tick marks, and the tick intervals labeled one through five and the last*
- 352 [*tick has 100 over it. Writes three squiggly lines along number line. Then writes "10"*
- 353 [*and circles it. Types 10 into Rabbit-speed Box and activates it. Counts the seconds it*
- 354 [*takes the rabbit softly to itself.*] Yep, that's too slow. [*Writes "+10" next to the*
- 355 [*circled 10. Writes "20" and puts scratch marks around it.*]
- 356 Bill: How long is it going to take?
- 357 10:14 Ann: Twenty, twenty seconds. [*Writes "20" again, this time boldly, and circles it.*]
- 358 ...Okay.
- 359 Bill: [*Pause*] You're exactly right. Is there some relationship here [*Ann yawns*] ...that you,
- 360 say, remember the first ones that we were doing when we had a set speed, and you
- 361 were calculating the time? All we're doing is the reverse of that now [*flips hand*
- 362 [*around and shows its backside*]. Do you have any ideas as to how you might
- 363 approach getting these, figuring out what speed it has to be?
- 364 Ann: [*Quickly*] No [*shakes head slightly and chuckles*].
- 365 Bill: Okay. That's all right. [*Ann types in 20 and activates rabbit*] So twenty is your bet
- 366 today, right? He's off and running. [*They watch it go. Before it's done, Ann writes 20*
- 367 [*on the answer sheet*]. You knew that one for sure, right?
- 368 10:15 Ann: Yeah. As soon as it went half way...
- 369 Bill: [*Interrupting*] Let me ask you before you do this next one, let's say he's running it at
- 370 uh...40 feet per second. How long is it going to take him to go over and back?
- 371 Ann: [*Looking down at the problem sheet*] Forty feet per second?
- 372 Bill: Yeah. [*Pause*] It's not one of them listed there [*gestures to problem sheet*], I don't
- 373 think. From the others we were doing earlier, you know, we were setting the speed
- 374 and seeing how long it took him. How long should it take if you set it for forty feet
- 375 per second?
- 376 10:16 Ann: Forty feet per second... [*Searches through scratch paper. Pauses. Uses calculator for*
- 377 [*100÷40*] 2.5 seconds to get there and 2.5 seconds to get back.
- 378 Bill: Yeah [*nods*] You see, that was this one right here [*points to one of the previous*
- 379 [*problems Ann did*]. Let's go on with the next one, I wanted to go back and make sure

380 that you understood about what we were doing before and you do so that's fine. How
 381 about eight seconds? How long is it going to take him, or what speed, I mean, shall he
 382 have to race at to get there and back in eight seconds.

383 10:17 Ann: [*Long pause while searching through scratch paper*] Twenty-five.

384 Bill: Okay, let's set him and see [*Ann puts 25 into the Rabbit-speed Box*]. Now how did
 385 you come up with that?

386 Ann: I-I looked back here [*holds up old scratch paper*] and this is, we're talking about
 387 eight seconds, four plus four is eight, and I got that when I was trying to figure out
 388 how long it would take the speed of twenty-five.

389 Bill: [*Looking at Ann's paper*] Ah, okay [*nods*], all righty. [*Pause*] Okay, you want to run
 390 the rabbit [*Ann activates rabbit*]. I wonder what it would do if we just ran it with the
 391 turtle's [*points to Turtle-Over Box*] saying zero speed over and forty back [*chuckles*].
 392 Maybe that's why it's giving us that smiley face. [*They watch the race end*] What are
 393 we aiming for?

394 Ann: Eight seconds.

395 Bill: Eight seconds, right on the button. Good for you. [*Ann writes "8" on the answer*
 396 *sheet*]

397 Six is next [*meaning give Rabbit a speed that would make him go over and back in 6*
 398 *seconds*]

399 Ann: We didn't do that one.

400 Bill: Huh?

401 Ann: We haven't done that one [*meaning that six seconds was not a previous result from*
 402 *Activity I*].

403 Bill: Uh uh [no].

404 Ann: Notes don't help [*chuckles, rearranging her scratch paper.*]

405 Bill: But that's all right. There's plenty of paper there. We've got plenty of space to write.

406 Ann: Okay. Six ... [*writes $100 \div 15$ in long division form, then uses the calculator to find*
 407 *the result*]¹

408 Bill: So, what did you do, divided fifteen into a hundred?

409 Ann: [*Looks quizzically at the result*]. That's wrong. [*Responding to Bill's question:*] Yeah.

410 Bill: That was for a guess-and-test kind of thing?

411 Ann: Yeah. [*Writes "6.6"*].

412 Bill: Okay. And what did you come up with for that?

413 Ann: Six point six, that's over already, and that's for just one way.

414 Bill: Ah.

¹ We use an ellipsis (...) within excerpts to indicate a pause. It does not indicate omitted text.

- 415 Ann: [*Pause. Then she mumbles:*] 100 divided by 10 seconds... [*writes $100 \div 10$ in long*
 416 *division form in the upper left corner of the scratch paper. Then she looks like she*
 417 *might solve it by hand, but then she uses the calculator for the result. Looks at the*
 418 *display for a moment, then hits the "clear" button on the calculator.*]
- 419 10:19 Bill: That hundred divided by ten gave you ten? [*Pause*] Is that right?
 420 Ann: [*Uses calculator again for $100 \div 10$*] Yeah.
 421 Bill: That's right. Ten times ten is a hundred. Can you think of a more efficient way, rather
 422 that having to go down and guess and check and guess and check... This would work.
 423 There's nothing wrong with it [*shrugs shoulders*]. But is there a quicker or more
 424 efficient way of doing it do you think?
 425 Ann: Yeah. [*Begins to scribble on page aimlessly*] There is, but I can't do it that way.
 426 Bill: Oh, what way is that? Oh, 'cause you don't know what it is yet?
 427 Ann: Look at the answer book.
 428 Bill: Oh [*chuckling*]
 429 Ann: We don't have an answer book [*puts pencil down*].
 430 10:20 Bill: No, there isn't an answer book for this stuff.
 431 Ann: So...
 432 Bill: That's true. [*Ann uses the mouse and keyboard to enter 5 in the Rabbit-speed Box and*
 433 *activates it.*] Now if you... From before, if you set him for five miles, err five feet per
 434 second, how long would it take him to get over there [*gestures with hand over*]?
 435 Ann: [*To self :*] Five feet per second. [*To Bill :*] Over six seconds.
 436 Bill: Yeah.
 437 Ann: Well over six seconds [*nervously plays with hands*].
- 438 Bill: But the way you were doing it before [*gestures to scratch paper*], you know, the first,
 439 the first things we were working on here. How did you figure out how long it would
 440 take him?
 441 Ann: We didn't do it ... last time. [*meaning 6 seconds*]
 442 Bill: I know we didn't do it with five seconds, but how did you figure out how long it
 443 would take him if he has a set speed [*points to Rabbit-speed Box*], in this case of five
 444 feet per second?
 445 Ann: I ... added. I think. I don't know.
 446 Bill: On all the first problems you were doing, all these [*points to first piece of scratch*
 447 *paper having Ann's calculations*]?
 448 Ann: No, I divided.
 449 Bill: Yeah.
 450 Ann: For the [*inaudible*], for the time ones, to find out the time.

451 Bill: Okay. So if I divide the ... What is this time [*points to the Rabbit-speed Box*] going to
452 come up with? Can you tell?

453 Ann: Umm [*looking to the computer screen*] About forty seconds, probably.

454 Bill: Yep [*nods*] Does that sound right to you?

455 Ann: No [*chuckles*]. That's way too far.

456 Bill: True. [*Pause*] So, what is it ... [*Ann plays with the mouse*] Let's go back and review
457 again. What is the target time we're aiming for here?

458 Ann: ...Umm...Six seconds.

459 Bill: Okay [*nods slightly*]. And we know five is moving way too slow, right?

460 Ann: [*Nods*] Yeah.

461 Bill: Was ten moving too slow?

462 Ann: ...Yeah.

463 Bill: Yeah. [*Pause*] And fifteen was too fast. Or was that too slow?

464 Ann: [*Looks down to the scratch paper*] I don't know. No, it was too slow.

465 Bill: We're aiming for six seconds now, [*points it on the scratch paper*] right?

466 Ann: Uh huh [*looks back to scratch paper then to the problem set three times*]

467 Bill: And how long did you calculate that it would take him to go over...running at fifteen
468 feet per second? Your calculation's right down there [*points to it on the scratch*
469 *paper*].

470 10:22 Ann: It's 6.6 just to go one way.

471 Bill: So,...that's still too slow, isn't it?

472 Ann: Yeah.

473 Bill: [*Nods*] Okay. So which direction do we have to go, above or below?

474 Ann: Above [*pointing up*].

475 Bill: [*Nods*] Okay. And if he ran twenty feet per second...[*Ann immediately types 20 in the*
476 *Rabbit-speed Box.*] You already figured that one out what he's going to get, right
477 [*Ann activates the rabbit, and waits for it to give her the result*]?

478 Ann: He would get...five seconds, no.

479 Bill: Five over..., [*waiting for a response*].

480 Ann: ...five back [*rabbit finishes*].

481 Bill: And that's still too slow, isn't it?

482 Ann: [*Pause, then tries 30 for the rabbit, watching it go*] It's too fast. Maybe. Maybe not.
483 [*Rabbit finishes*] Too slow. [*Tries 31 for the rabbit. It still comes in too slow*]

484 10:23 Bill: You're getting closer though. [*Ann pauses while thinking. Then she types 32 and tries*
485 *to change it*] You have to go to backspace, I think, to erase the two [*referring to the*
486 *second digit of 32*].

- 487 10:24 Ann: [*Changes the Rabbit-speed to 33. Watches the rabbit go.*] That would be right.
488 [*Rabbit finishes*] How can you minus this one-tenth of a second?
- 489 Bill: Does he have to run right at thirty-three? Or twenty? Or twenty-five? Can he run a
490 part of a feet per second in terms of speed? Like 33.1?
- 491 Ann: Probably.
- 492 Bill: Yeah [*nods*], we can go in there and see. [*Both move forward to type on the keyboard*]
493 Well, go ahead [*Ann types 33.1 and activates the rabbit. They watch it go.*] Good
494 shot. Now, we're almost out of time, we've only got about a minute left, it looks like
495 [*Ann writes "33.1" in the ft/sec. column next to 6 sec. on the problem set page*]. Ann,
496 what I'd like you to think about...there's no assigned homework on this tonight.
497 Umm...but you know the way we were going [*moves hand over the distance line*]
498 first of all, we had a set speed and you were trying to figure out what the time was.
499 And now we're going the other way around, and what I'd just like you to think about
500 over the evening: Is there a more efficient way to do this [*points to the problem*
501 *sheet*], this reverse process, instead of having to guess and check? And we'll pick up
502 where we left off tomorrow [*Ann nods*]. Anything else you want to try on the thing
503 [*Note: computer*] while we've got a few minutes or seconds left?
- 504 10:25 Ann: Yeah.
- 505 Bill: What do you want to do? [*Ann types ".1" for the Rabbit-speed Box and activates the*
506 *Rabbit.*]. Oh, you want to be here for a long time.
- 507 Ann: I want to see how long this will take.
- 508 Bill: Well, you should be able to calculate it out can't you do that the way you were doing
509 the first ones?
- 510 Ann: Yeah, but I just want to see. I like... He's not going to get back very quick.
- 511 Bill: No, I think the bell's going to ring before he even gets down there [*Note: to the 100 ft*
512 *tick mark*] to be honest with you. From that [*gestures toward the computer screen*]
513 can you calculate how long it should take him? You've got the calculator there. Feel
514 free to use it.
- 515 Ann: Over forty seconds.
- 516 Bill: Forty?
- 517 Ann: Over forty.
- 518 Bill: Over, I would believe that. How far has it gone so far?
- 519 Ann: Not even a foot and it's at twenty seconds.
- 520 Bill: Each one of these [*points to a tick mark*] are how far?
- 521 10:26 Ann: That's ten feet.
- 522 Bill: Okay, so he hasn't even gone ten feet yet and it's twenty-five seconds so far. So can
523 you figure out ho-how long it's going to take him.
- 524 Ann: Maybe.
- 525 Bill: Give it a try, 'cause we're out of time anyway.

- 526 Ann: Fifty seconds. No. Sixty, sixty seconds.
- 527 Bill: No. It's going to be a lot more than that. He hasn't even gone ten feet and it's already
528 [*points to the Time Counter*] up to thirty-five. Thirty, sixty, ninety, it's going to be
529 whole bunches.
- 530 Ann: I know! Um, two hundred seconds. Two hundred.
- 531 Bill: Well, maybe we'll find out when we come back next time. But right now you've got
532 to go to class.